

Name: \_\_\_\_\_

Date: \_\_\_\_\_

Period: \_\_\_\_\_

## Chapter 11: Coordinate Geometry Proofs

### Topic 8: Rectangle Proofs

#### **Do Now:**

Given line  $\overline{AB}$  with endpoints  $A(0, 6)$  and  $B(-2, -2)$ , and line  $\overline{CD}$  with endpoints  $C(2, 0)$  and  $D(0, -4)$ , are these lines parallel, perpendicular, or neither? Explain your answer.

**Recall:** A **rectangle** is a quadrilateral in which both pairs of opposite sides are parallel and congruent, and all four angles are right angles.

#### **Properties of Rectangles:**

- All the properties of a parallelogram.
- One right angle.
- Diagonals \_\_\_\_\_.

**To prove that a Quadrilateral is a Rectangle, we must prove that**

\_\_\_\_\_ (midpoint twice).

\_\_\_\_\_ (distance twice).

**Examples:**

1. Prove that quadrilateral A(4, 4), B(6, 1), C(0, -3), and D(-2, 0) is a rectangle.

- Plot and label the graph
- Midpoint & Work

Conclusions:

$\therefore \overline{AC}$  bisects  $\overline{BD}$  because \_\_\_\_\_

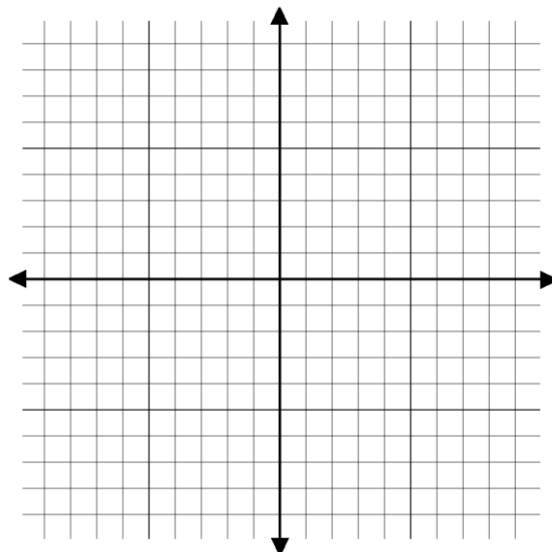
$\therefore$  Quadrilateral ABCD is \_\_\_\_\_

- Distance & Work

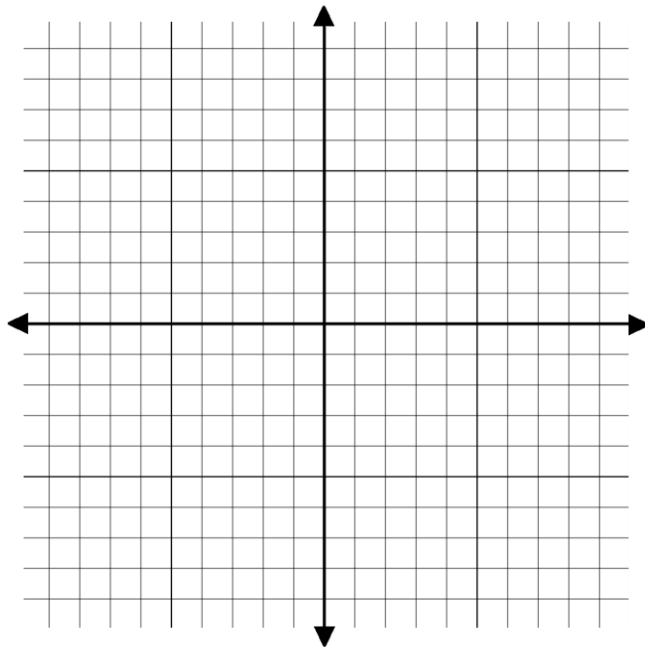
Conclusions:

$\therefore \overline{AC}$  is congruent to  $\overline{BD}$  because \_\_\_\_\_

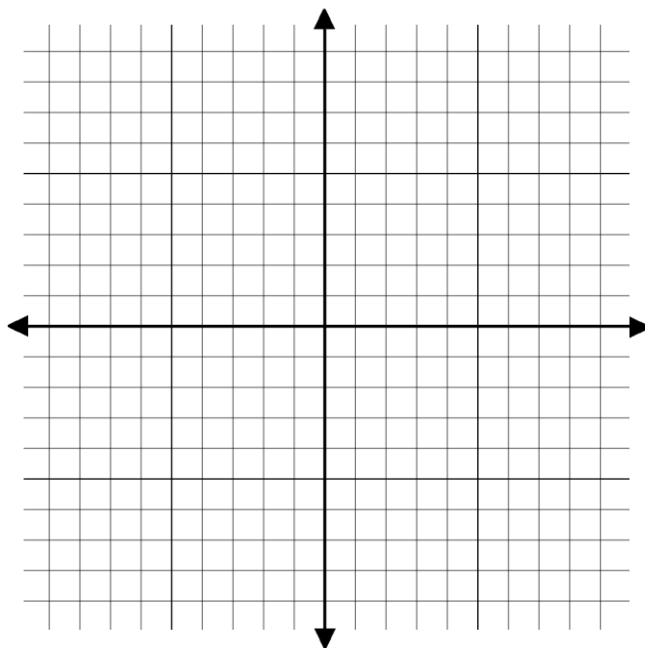
$\therefore$  Parallelogram ABCD is \_\_\_\_\_



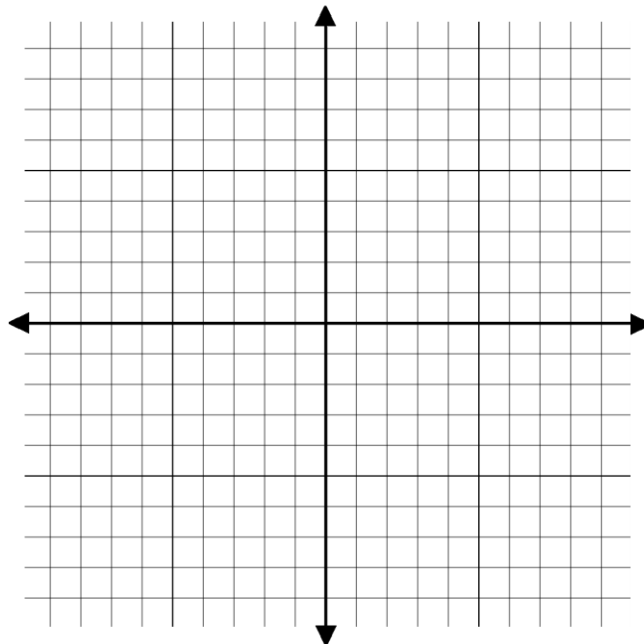
2. Determine if quadrilateral PQRS with  $P(0, 2)$ ,  $Q(4, 8)$ ,  $R(7, 6)$  and  $S(3, 0)$  is a rectangle.



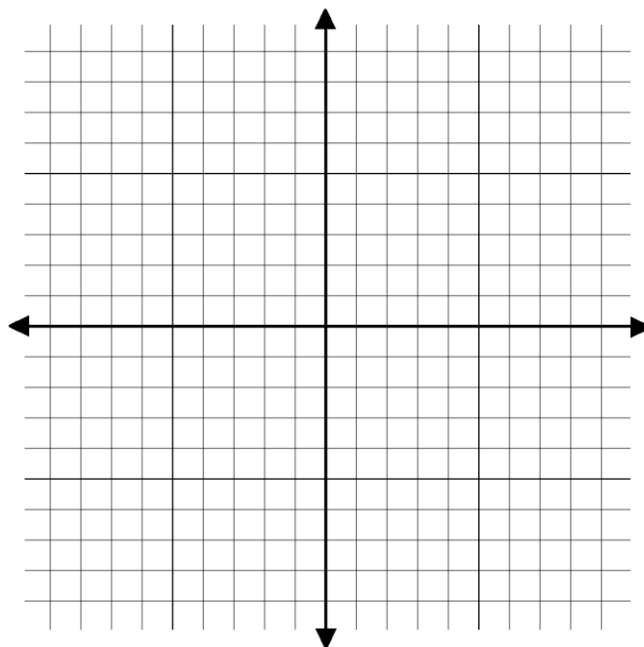
3. Determine if quadrilateral WXYZ with  $W(1, 2)$ ,  $X(-4, 8)$ ,  $Y(-8, 6)$ , and  $Z(-3, 0)$  is a rectangle.



4. Prove that Quadrilateral EFGH with E(1, 4), F(7, 0), G(5, -3) and H(-1, 1) is a rectangle.



5. **Given:** A(-5, 6), B(6, 6), C(8, -3), D(-3, -3)  
**Prove:** This quadrilateral is a rectangle.



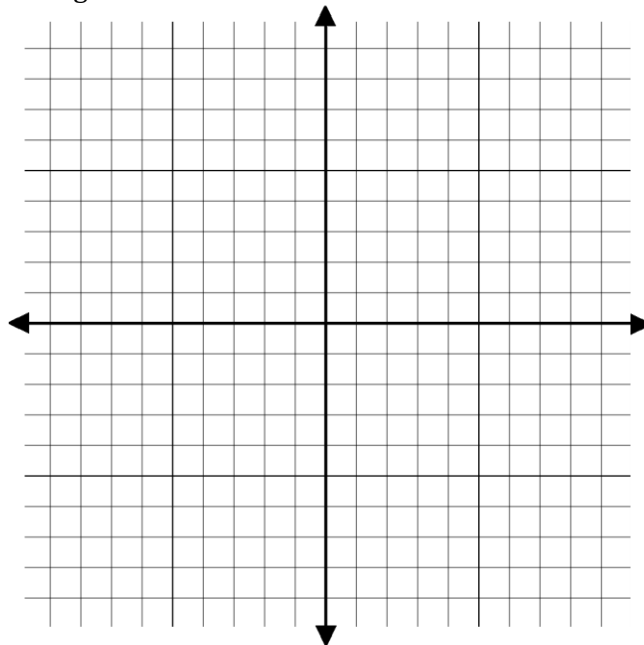
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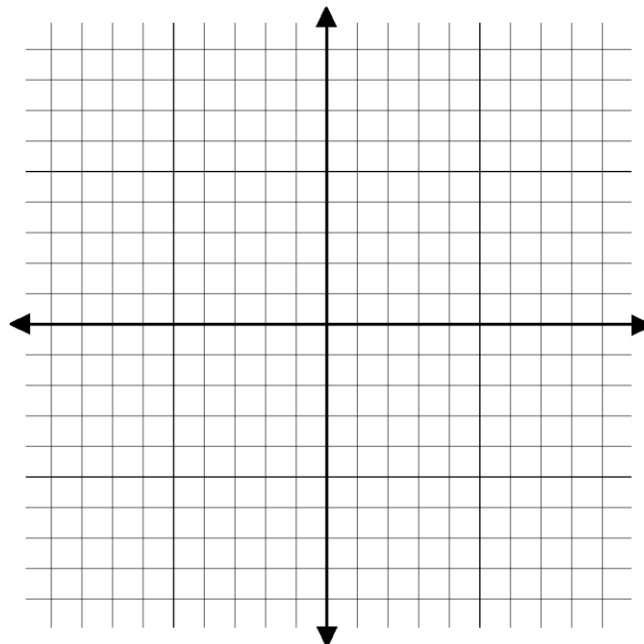
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### Rectangle Proofs Homework

1. Prove that  $W(-5, -1)$ ,  $X(-4, 3)$ ,  $Y(8, 0)$  and  $Z(7, -4)$  is a rectangle.



2. Determine if quadrilateral PQRS with  $P(-7, 3)$ ,  $Q(-5, 7)$ ,  $R(-1, 3)$  and  $S(1, 7)$  is a rectangle.



3. The coordinates of the endpoints of  $\overline{FG}$  are  $(-4, 3)$  and  $(2, 5)$ . Find the length of  $\overline{FG}$  in simplest radical form.