

Chapter 11B: Coordinate Geometry Triangle Proofs
Topic 1: Classifying Triangles

Recall the classifications of triangles:

By Sides:

- **Scalene** Triangle: All three sides of the triangle have different lengths.
- **Isosceles** Triangle: Two of the three sides of the triangle have the same length.
- **Equilateral** Triangle: All three sides of the triangle have the same length.

To classify any triangle by its SIDES use: _____

By Angles:

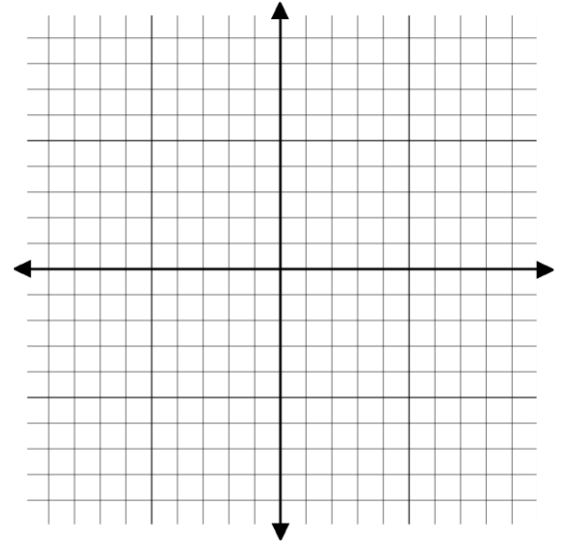
- **Right** Triangle: One right angle
- **Acute** Triangle: All acute angles
- **Obtuse** Triangle: One obtuse angle

To classify a RIGHT triangle use: _____

Then _____

Practice Examples:

- 1) The coordinates of the vertices of $\triangle ABC$ are $A(-5,3)$, $B(-1,-2)$ and $C(2,3)$. Show that $\triangle ABC$ is scalene.

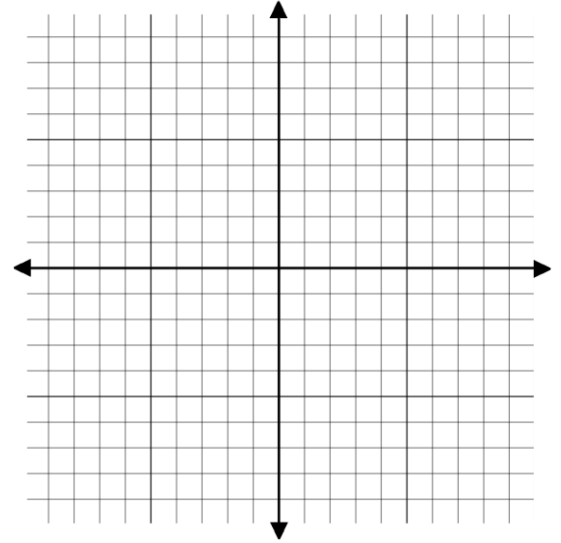


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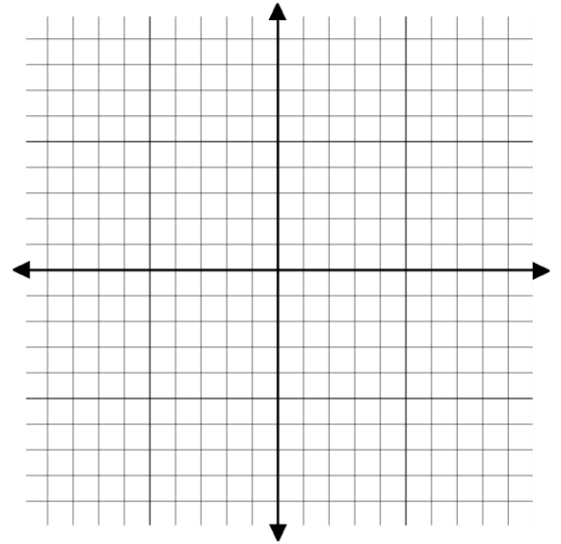
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2) Given $\triangle HIJ$ with $H(5,2)$, $I(6,1)$ and $J(8,4)$. Using coordinate geometry prove that $\triangle HIJ$ is an isosceles triangle.



3) If the vertices of $\triangle PQR$ are $P(-6, -5)$, $Q(4, -5)$ and $R(4, -1)$, show that it is a right triangle.

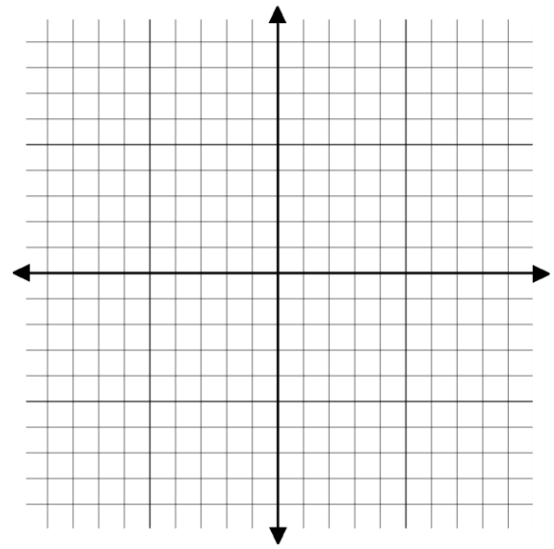


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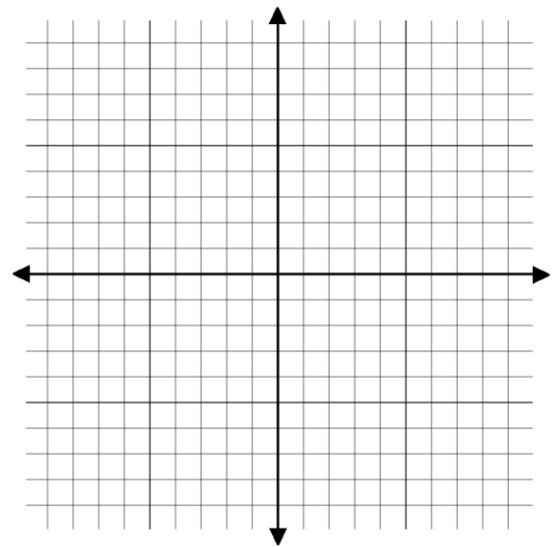
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4) If the vertices of $\triangle PQR$ are $P(0,0)$, $Q(2,0)$ and $R(1,3)$, classify the triangle.



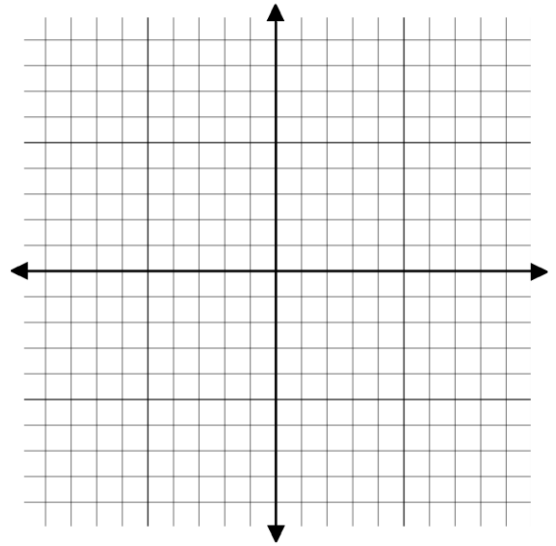
5) The coordinates of the vertices of $\triangle HIJ$ are $H(-3,3)$, $I(1,-3)$ and $J(3,7)$. Using coordinate geometry prove that $\triangle HIJ$ is an isosceles right triangle.



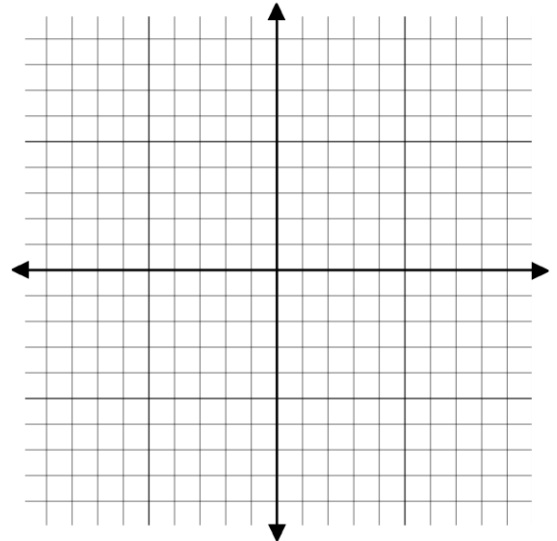
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Chapter 11B: Coordinate Geometry Triangle Proofs
Topic 1 Homework

- 1) The coordinates of the vertices of $\triangle ABC$ are $A(-3, -1)$, $B(-1, 7)$ and $C(2, 1)$. Show that $\triangle ABC$ is a scalene triangle.



- 2) If the vertices of $\triangle DEF$ are $D(-6, 3)$, $E(-2, 3)$ and $F(0, 1)$, show that $\triangle DEF$ is not an isosceles triangle.

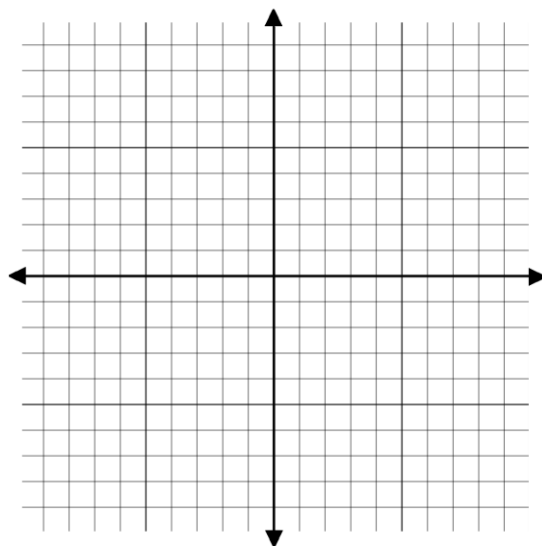


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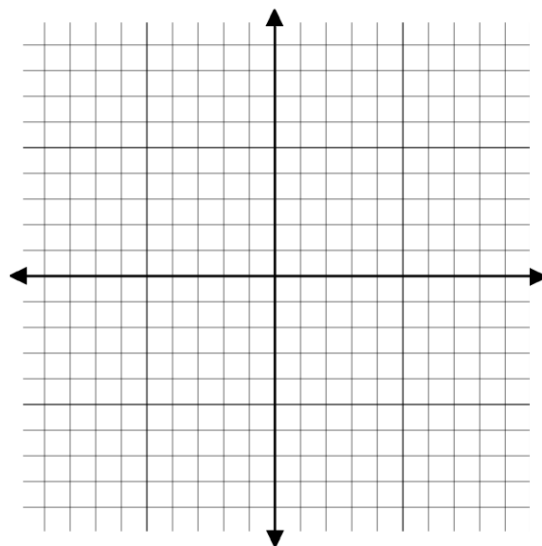
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- 3) If the coordinates of the vertices of ΔPQR are $P(6, 4)$, $Q(-2, 9)$ and $R(3, 7)$. Using coordinate geometry classify the triangle.



- 4.) The coordinates of the vertices of ΔVAC are $V(-9, -2)$, $A(-3, 4)$ and $C(3, -2)$. Using coordinate geometry prove that ΔVAC is an isosceles right triangle.

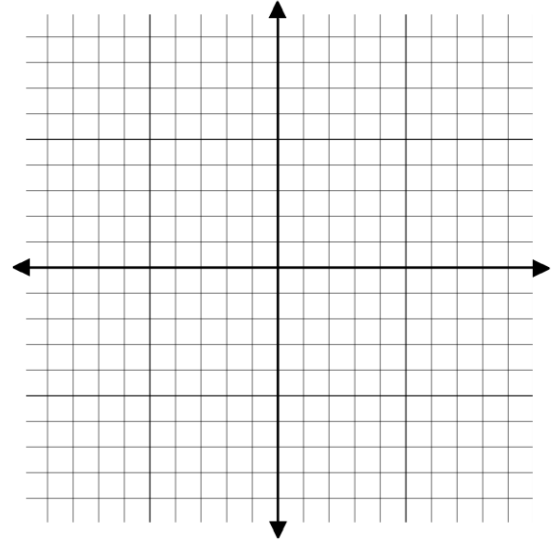


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5.) If the coordinates of the vertices of $\triangle HIJ$ are $H(0, -2)$, $I(5, -2)$ and $J(0, 10)$. Classify the triangle by side and angle.



Extra examples if you need more practice

- 1) The coordinates of the vertices of $\triangle ABC$ are $A(5, 4)$ $B(2, 7)$ and $C(-3, 6)$. Show that $\triangle ABC$ is a scalene triangle.
- 2) If the coordinates of the vertices of $\triangle DEF$ are $D(8, -2)$ $E(-4, 6)$ and $F(1, 5)$. Using coordinate geometry classify the triangle.
- 3) If the coordinates of the vertices of $\triangle DEF$ are $D(2, 3)$ $E(0, 0)$ and $F(4, 0)$. Show that $\triangle DEF$ is an isosceles triangle.
- 4) If the coordinates of the vertices of $\triangle STU$ are $S(-4, 3)$ $T(4, 3)$ and $U(0, 8)$. Using coordinate geometry classify the triangle.
- 5) If $\triangle WXY$ has the vertices $W(3, 4)$ $X(3, 8)$ and $Y(6, 4)$, classify the triangle.
- 6) If the vertices of $\triangle LMN$ are $L(4, -1)$ $M(5, 6)$ and $N(1, 3)$ show that $\triangle LMN$ is an isosceles right triangle.

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Coordinate Geometry Triangle Proofs (HW)

$$1) \begin{aligned} AB &= \sqrt{68} \\ BC &= \sqrt{45} \\ AC &= \sqrt{29} \end{aligned}$$

$$2) \begin{aligned} DE &= \sqrt{16} \\ EF &= \sqrt{8} \\ DF &= \sqrt{40} \end{aligned}$$

$$3) \begin{aligned} PQ &= \sqrt{89} \\ QR &= \sqrt{29} \\ PR &= \sqrt{18} \\ \therefore & \text{ scalene} \end{aligned}$$

$$4.) \begin{aligned} VA &= \sqrt{72} \\ AC &= \sqrt{72} \\ VC &= \sqrt{144} \end{aligned}$$

$$5.) \begin{aligned} HI &= \sqrt{25} \\ IJ &= \sqrt{169} \\ HJ &= \sqrt{144} \end{aligned}$$

\therefore Scalene Right

\therefore not Isosceles Right

$$1) \begin{aligned} AB &= \sqrt{18} \\ BC &= \sqrt{26} \\ AC &= \sqrt{68} \end{aligned}$$

$$2) \begin{aligned} DE &= \sqrt{208} \\ EF &= \sqrt{26} \\ DF &= \sqrt{98} \end{aligned}$$

$$3) \begin{aligned} DE &= \sqrt{13} \\ EF &= \sqrt{16} \\ DF &= \sqrt{13} \end{aligned}$$

$$4) \begin{aligned} ST &= \sqrt{64} \\ TU &= \sqrt{41} \\ SU &= \sqrt{41} \end{aligned}$$

$$5) \begin{aligned} WX &= \sqrt{16} \\ XY &= \sqrt{25} \\ WY &= \sqrt{9} \end{aligned}$$

$$6) \begin{aligned} LM &= \sqrt{50} \\ MN &= \sqrt{25} \\ LN &= \sqrt{25} \end{aligned}$$